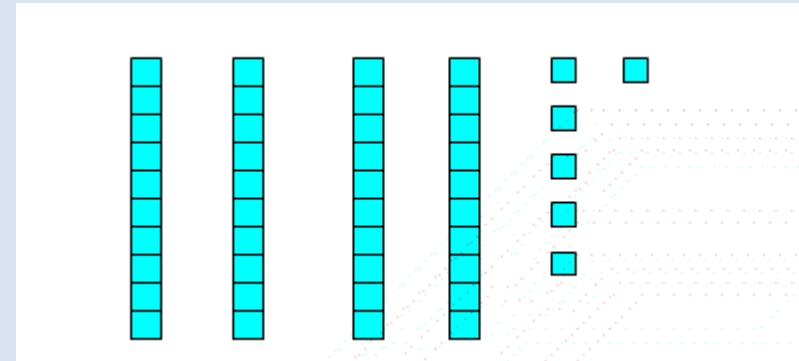


# Sequence of learning

Autumn	Number: Place value	Number: Addition and Subtraction		Measurement: Money	Number: <u>Multiplication</u> and Division	
Spring	Number: Multiplication and <u>Division</u>	Statistics	Geometry: Properties of Shape	Number: Fractions		Measurement: length and height Consolidation
Summer	Position and direction	Problem solving and efficient methods	Measurement: Time	Measurement: Mass, Capacity and Temperature		Investigations

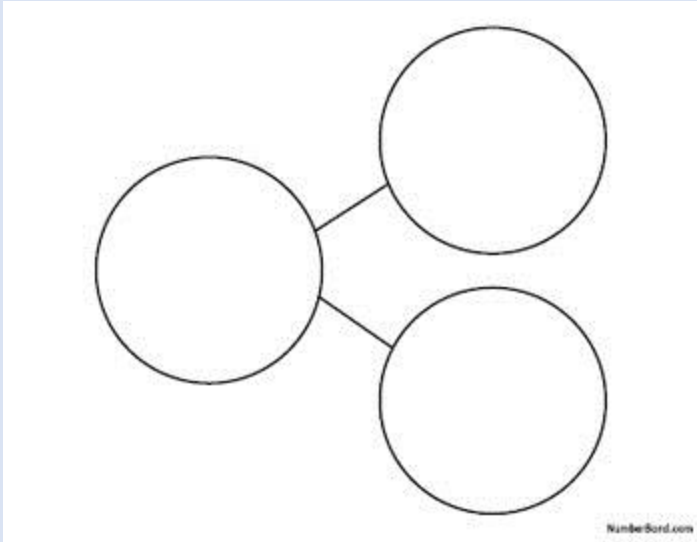
# Concrete apparatus

All lessons start with concrete apparatus. Children need to visually see and physically feel the calculation process. Through each method I will aim to show you how we use the concrete apparatus. I know you don't have this at home, but on the internet there are some resources you can use. Lego and money can also be useful at time.

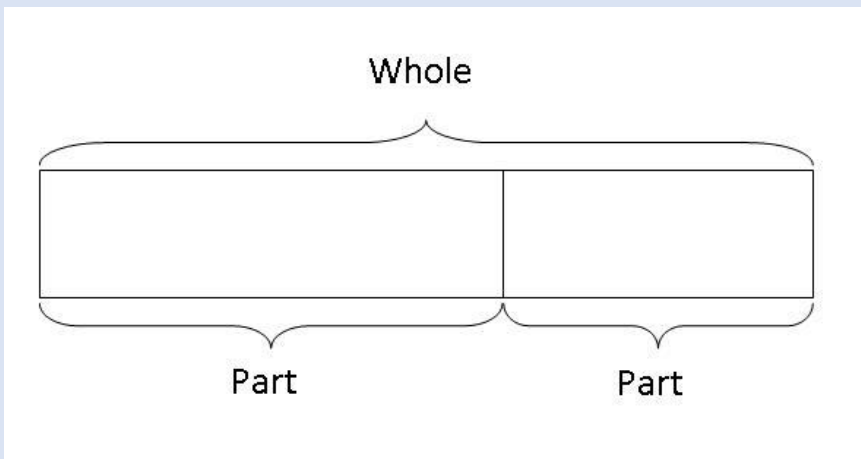


<https://www.topmarks.co.uk/Flash.aspx?f=diennesandcoinsv3>

# Models



$$100 - 30 = 70$$



<p><b>Part-Part-Whole</b></p> <p>Whole</p> <p>Part      Part</p> <p>Whole = Part + Part Part = Whole - Part</p>	<p><b>Equal Parts of a Whole</b></p> <p>Whole</p> <p>Part    Part    Part</p> <p>Whole = Part x Number of Parts Part = Whole ÷ Number of Parts Number of Parts = Whole ÷ Part</p>
<p><b>Comparison</b></p> <p>A</p> <p>B      Difference</p> <p>Difference = A - B A = B + Difference</p>	<p><b>Part-Part-Whole and Comparison</b></p> <p>A</p> <p>B      Difference</p> <p>Whole</p> <p>Whole = A + B Difference = A - B</p>

# Warm up

- If I know  $3+7$  I also know....

$$30+70=100$$

$$13+7=20$$

$$10-3=7$$

$$100-30=70$$

It is important children know number bonds and facts and use related facts to support them in calculation. It will make them more efficient in their processes.

# Using a blank number line

- $24+8=$  (crossing tens boundary)
- $=75-7$  (crossing tens boundary)
- $34p+42p=$  (not crossing tens boundary)
- $=64-32$  (not crossing tens boundary)
- $5 \times 7=$  (use knowledge of commutativity)
- $=44 \div 5$
  
- How can we use equipment to model?
  
- This is why number bonds and confident counting are important and these skills need to be continually revisited.

# Finding the difference

- When looking at a calculation children need to begin to decide upon which is the most efficient way to calculate.
- When subtracting if they notice the two numbers are close together they are find the difference between the two numbers rather than counting backwards.

$12-9=$

$25-21=$

# Partitioning for addition and subtraction

- Without crossing the tens boundary

$$25 + 33 = \quad = 78 - 25$$

Crossing tens boundary

$$25 + 33 = \quad = 78 - 25$$

How can we use equipment to model?

How can we use drawing to model?

$$34 - 13 =$$
$$\begin{array}{r} 34 \\ / \quad \backslash \\ 30 \quad 4 \\ -10 \quad -3 \\ \hline 20 \quad 1 \end{array}$$

$$42 - 15 =$$
$$\begin{array}{r} 42 \\ / \quad \backslash \\ 40 \quad 2 \\ -10 \quad -5 \\ \hline 30 \quad 7 \end{array}$$

We can't subtract the ones. Can we partition differently?

$$\begin{array}{r} 42 \\ / \quad \backslash \\ 30 \quad 12 \\ -10 \quad -5 \\ \hline 20 \quad 7 \end{array}$$

Now we can subtract the ones and then subtract the tens.  
 $42 - 15 = 27$

# Column method

- With Base 10.
- Pictorial representation
- Formal method

Tens	Ones
	..

23
+ 40
63

Tens	Ones
	...

56
- 30
26

Tens	Ones
	.....
	.....

28
+ 7
35
1

Tens	Ones
/	.....
	.....

<del>1</del> 14
- 8
6

		..
+		..
		..

		...
+		...
		...

64
+ 17
81

28
- 13
15

Tens	Ones
/	.....
	.....

<del>2</del> 14
- 16
18



# Pictorial method for multiplication and division

- Drawing arrays

$$24 \div 2 = \quad \quad \quad 12 \times 5 =$$

- Sharing and grouping

$$20 \div 5 =$$

Results will be the same.

$$11 \times 5$$

Could work out as...

$$10 \times 5 = 50 \text{ so } 11 \times 5 \text{ must equal } 55$$

Confidence in counting sequence really does support and using fingers or marks on paper to keep track.

# Missing Numbers

- Inverse relationship – if children are familiar with this by writing fact families it will support them in encouraging them to use this know when solving missing numbers.

$$23 + \underline{\quad} = 47$$

$$\underline{\quad} - 43 = 36$$

$$3 \times \underline{\quad} = 15$$

$$60 \div \underline{\quad} = 12$$

# Balance equations

- $15+24=8+31$
- $45-23=15+7$
- $5 \times 2 = 1 \times 10$
- $32-21 = \underline{\quad} - 34$

# Worded questions

- **Sam is collecting cards. He wants to collect 100 cards altogether. Last week he collected 50 cards. This week he collects 30 cards. How many more cards does he need?**
- **Amy plants 4 rows of carrots. There are 3 carrots in each row. A rabbit eats 2 of the carrots. How many carrots are left?**
- **Sita has 50 raisins. She gives 23 to Ben. She gives 15 to Amy. How many raisins does Sita have left?**
- **There are 29 children on the school bus. 2 boys and 6 girls get off. How many children are left on the bus?**
- **A lollipop costs 35p. Ben gives the shopkeeper 50p. How much change should Ben get?**

# Finally...

- You may have noticed calculations are presented in different ways. It is important children are used to it.
- It is great if children can calculate mentally (without necessarily recording anything) and this should be praised. It is important though that they do know a way to record the processes they calculate in their head, so they can share with others. Explaining and reasoning are important aspects of the curriculum.
- Checking answers – can they make an estimate prior to calculating e.g  $25+22=$  will be near 50 because I know double 25=50. This will help them see if their answer could be correct.
- Game give them a set of calculations on post-its and they need to sort them into two piles – those that are correct and those that are incorrect. Then have a conversation about children's thoughts and reasons. Discuss calculation processes they have used.